

• Candidates should be able to :

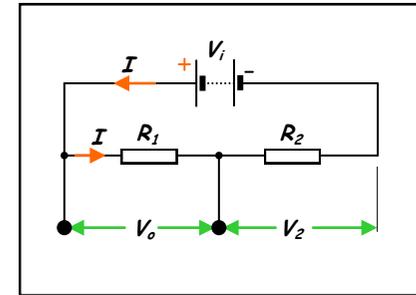
- Draw a simple *potential divider circuit*.
- **Explain** how a potential divider circuit can be used to produce a variable pd.
- **Recall and use** the potential divider equation :

$$V_{out} = V_{in} \times \frac{R_2}{(R_1 + R_2)}$$

- Describe how the resistance of a *light-dependent resistor (LDR)* depends on the intensity of light.
- Describe and explain the use of *thermistors and LDRs* in *potential divider circuits*.
- Describe the *advantages* of using *data-loggers* to monitor physical changes.

• SUPPLYING A FIXED PD

The simplest potential divider circuit (shown opposite) is one which uses two resistors in series to give a smaller, fixed pd from a larger pd.



For the circuit shown, the **current (I)** through  $R_1$  and  $R_2$  is given by :

$$I = \frac{\text{pd across the resistors}}{\text{total resistance}} = \frac{V_i}{R_1 + R_2}$$

$$\text{pd across resistor } R_1 = V_o = IR_1 = \frac{V_i R_1}{R_1 + R_2}$$

$$\text{pd across resistor } R_2 = V_2 = IR_2 = \frac{V_i R_2}{R_1 + R_2}$$

$$\text{So, } \frac{V_o}{V_2} = \frac{V_i R_1 / (R_1 + R_2)}{V_i R_2 / (R_1 + R_2)} = \frac{R_1}{R_2}$$

**Therefore, the ratio of the pds across each resistor is equal to the ratio of the resistances.**

The **OUTPUT VOLTAGE** or PD ( $V_o$ ) across  $R_1$  is given by :

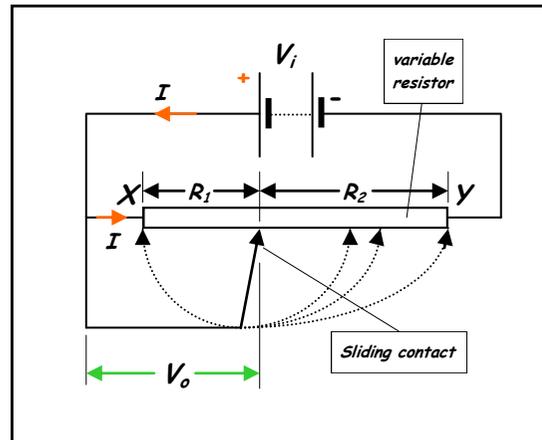
$$V_o = \frac{V_i R_1}{(R_1 + R_2)}$$

- For example, a pd of 12 V can be obtained from a 100 V supply by setting  $R_1$  at 1500  $\Omega$  and  $R_2$  at 11000  $\Omega$ .

$$V_o = \frac{V_i R_1}{(R_1 + R_2)} = \frac{100 \times 1500}{(1500 + 11000)} = \boxed{12 \text{ V}}$$

### SUPPLYING A VARIABLE PD

The potential divider circuit shown opposite uses a variable resistor to give a continuously variable output pd from a fixed input pd.



By moving the sliding contact on the variable resistor, the value of the **OUTPUT PD** ( $V_o$ ) can be adjusted:

- From a minimum of 0 V (sliding contact at position X).
- To the maximum value when it is equal to the **INPUT PD** ( $V_i$ ) (sliding contact at position Y).

The **OUTPUT VOLTAGE** or PD ( $V_o$ ) across  $R_1$  is given by:

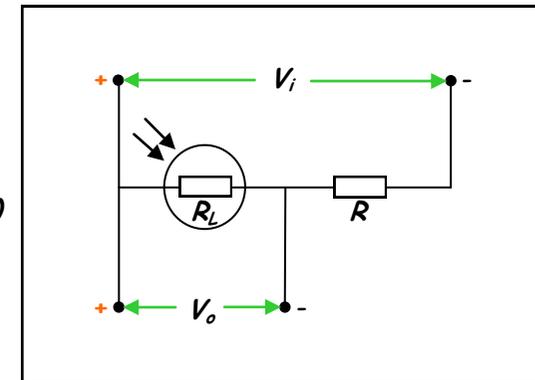
$$V_o = \frac{V_i R_1}{(R_1 + R_2)}$$

- With the sliding contact at position X,  $R_1 = 0 \Omega$ , so  $V_o = \boxed{0 \text{ V}}$
- With the sliding contact at position Y,  $R_1 = R$  (max. resistance of the variable resistor)

$$R_2 = 0 \Omega, \quad \text{so } V_o = \frac{V_i \times R}{(R + 0)} = \boxed{V_i}$$

### LIGHT-DEPENDENT POTENTIAL DIVIDER

The diagram opposite shows a **light-dependent resistor (LDR)** may be used in a potential divider to provide an **output pd** ( $V_o$ ) which varies with **light intensity**.



An LDR is a resistor made from semiconducting material in which electrons are liberated when light shines on the surface of the material.

In **total darkness**, the only free electrons are those 'shaken' free by thermal vibrations of the atoms, so the LDR's **RESISTANCE IS VERY HIGH**.

As the **light energy incident on the LDR is increased**, more and more electrons are liberated and this means that the LDR's resistance becomes increasingly **LOWER**.

The OUTPUT PD ( $V_o$ ) is given by :

$$V_o = \frac{V_i R_L}{(R_L + R)}$$

#### In BRIGHT LIGHT

$R_L$  is LOW ( $\approx 50$  to  $100 \Omega$ ) compared with  $R$ .  
So the output pd ( $V_o$ ) is VERY SMALL.

As the light intensity DECREASES,  $R_L$  INCREASES.

#### In TOTAL DARKNESS

$R_L$  is VERY HIGH ( $\approx 10 M\Omega$ ) compared with  $R$ .  
So the output pd ( $V_o$ ) has its MAXIMUM VALUE ( $\approx V_i$ ).

- Since the output pd depends on light intensity, this potential divider could be used to control any process which is **light-level** dependent.

At the simplest level, this could mean **automatically switching on street lights when darkness falls**. A switching circuit could be set to operate when  $V_o$  reaches a pre-determined value, corresponding to a particular light intensity level. If  $R$  were replaced by a **variable resistor**, it would allow some manual adjustment of the value of  $V_o$  at a particular light intensity. So, if for example, the street lights were set to switch on at  $V_o = \frac{1}{2} V_i$ ,  $R$  could be adjusted so that this occurred at any desired level of illumination.

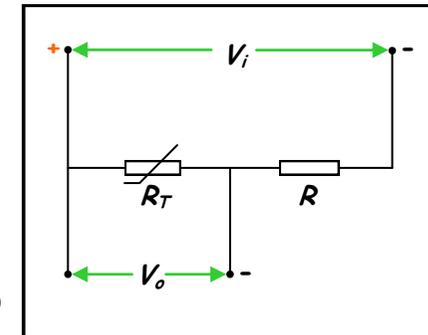
- If  $R$  and  $R_L$  were interchanged,  $V_o$  will **increase** as the **light intensity increases**. This could be used in a circuit to set off an alarm when a light is switched on or a safe is opened with the lights on.

- A **THERMISTOR** is a device whose resistance varies markedly with temperature.

With increasing temperature :

The resistance of a **negative temperature coefficient (NTC)** thermistor decreases.

The resistance of a **positive temperature coefficient (PTC)** thermistor increases.



- The OUTPUT PD ( $V_o$ ) is given by :

$$V_o = \frac{V_i R_T}{(R_T + R)}$$

For a **NTC** thermistor :

- When the temperature is HIGH,  $R_T$  is SMALL compared with  $R$  and so  $V_o$  will be SMALL.
- When the temperature is LOW,  $R_T$  is LARGE compared with  $R$  and so  $V_o$  will be LARGE.

- This **temperature-dependent** potential divider could form part of a circuit used to trigger a frost alarm or to switch on a heating system in order to keep the temperature above a certain value.

Replacing the fixed resistor  $R$  with a **variable resistor** allows manual adjustment of the 'trigger' temperature.

- If  $R_T$  and  $R$  are interchanged,  $V_o$  will then **increase** with **increasing** temperature. Such a potential divider could form part of a circuit used to switch on an air-conditioning system when the temperature exceeds a certain value.

#### • USE OF DATALOGGERS TO MONITOR PHYSICAL CHANGES

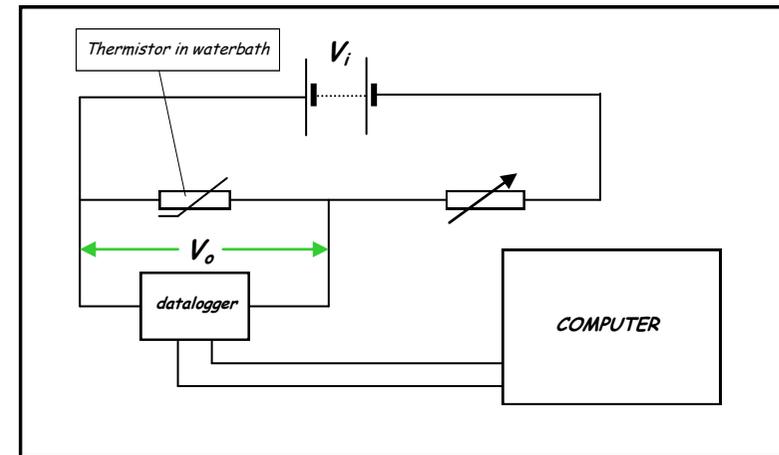
- The design of commercial **light** or **temperature-sensing** potential divider circuits requires a full knowledge of the relationship between the **output pd ( $V_o$ )** and either **light intensity** or **temperature**.

A **DATALOGGER** is a small, portable electronic device which enables data from an external sensor to be recorded over a given time period. It can be interfaced with a computer which analyses the data and displays the information graphically.

The advantages of a datalogger for monitoring physical changes are :

- The data is recorded automatically over any desired period.
- The collected data is continuously processed and displayed in a clear, graphical form.

#### USE OF DATALOGGER TO INVESTIGATE THE RELATIONSHIP BETWEEN OUTPUT PD ( $V_o$ ) AND TEMPERATURE



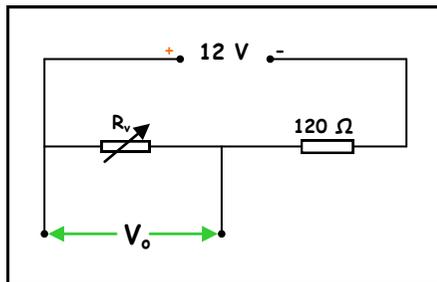
The circuit shown above may be used to investigate the variation of output pd ( $V_o$ ) with temperature for a **temperature-dependent** potential divider.

The datalogger's temperature sensor (i.e. the thermistor) is placed in a water bath whose temperature is gradually increased by heating it electrically.

One of the datalogger inputs records the changing water temperature and the second input records the output pd ( $V_o$ ) of the circuit. The two sets of continuously varying, corresponding readings are fed to a computer, which then analyses the data and displays the information as a graph.

• PRACTICE QUESTIONS

- 1 For the potential divider shown opposite, calculate the **range** over which the **output pd ( $V_o$ )** will vary when the variable resistor ( $R_v$ ) is adjusted from  $0 \Omega$  to  $720 \Omega$ .



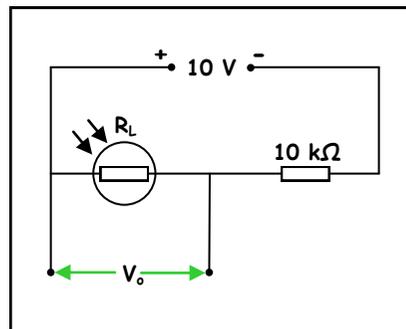
- 2 A potential divider consists of a  $2.5 \text{ k}\Omega$  resistor connected in series with a  $10 \text{ k}\Omega$  resistor and a battery of emf  $6.0 \text{ V}$  and negligible internal resistance.

(a) Draw the **circuit diagram** and calculate the **pd across each resistor**.

(b) If a  $5 \text{ k}\Omega$  resistor is then connected in **parallel** with the  $10 \text{ k}\Omega$  resistor, what will be the **pd values** across each resistor in this new circuit?

- 3 For the **light-dependent potential divider** circuit shown opposite, calculate:

(a) The **output pd ( $V_o$ )** when the LDR: (i) is in the **dark** and has a resistance of  $8.0 \text{ M}\Omega$ . (ii) is in **bright light** and has a resistance of  $200 \Omega$ .



(b) The **value of  $R_L$**  in lighting conditions for which  $V_o = 4.0 \text{ V}$ .

- 4 A light sensor consists of an LDR connected in **series** with a  $6 \text{ k}\Omega$  resistor and a  $6.0 \text{ V}$  battery. A high resistance voltmeter connected in parallel with the resistor, gives a reading of  $3.4 \text{ V}$  when the LDR is in **darkness**.

(a) Calculate the **pd across the LDR** and **its resistance** when the voltmeter reading is  $3.4 \text{ V}$ .

(b) A bright light is now shone on the LDR. **Describe** and **explain** the change observed in the voltmeter reading.

- 5 A potential divider consists of a  $1.5 \text{ k}\Omega$  resistor connected in series with a **thermistor** and a  $15 \text{ V}$  supply of negligible internal resistance.

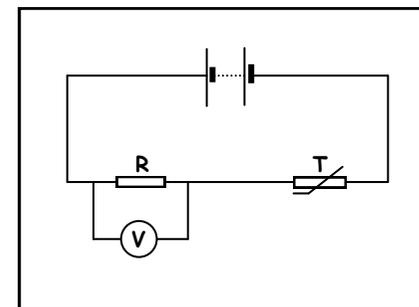
The **output pd ( $V_o$ )** is taken across the thermistor, whose resistance varies between  $120 \Omega$  at  $100 \text{ }^\circ\text{C}$  and  $6.0 \text{ k}\Omega$  at  $0 \text{ }^\circ\text{C}$ .

Calculate the output pd : (a) at  $100 \text{ }^\circ\text{C}$  (b) at  $0 \text{ }^\circ\text{C}$

• HOMEWORK QUESTIONS

- 1 The diagram shows a potential divider circuit used to monitor the temperature of a greenhouse.

The thermistor  $T$  is a **negative temperature coefficient** type. the voltmeter is placed across the resistor  $R$ .



**Describe** and **explain** how the voltmeter reading changes as the temperature of the greenhouse **increases**.

(OCR AS Physics - Module 2822 - January 2006)

(a) Kirchhoff's first law is based on the conservation of an electrical quantity. **State the law and the quantity conserved.**

(b) The diagram opposite shows a potential divider circuit. The battery has **negligible** internal resistance and the voltmeter has **very high** resistance.

(i) Show that the voltmeter reading is **1.5 V**.

(ii) An electric device rated at 1.5 V, 0.1 A is connected between the terminals X and Y. The voltmeter reading drops to a very **low** value and the device fails to operate, even though the device itself is not faulty.

1. Calculate the **total resistance of the device and the 400  $\Omega$  resistor in parallel.**

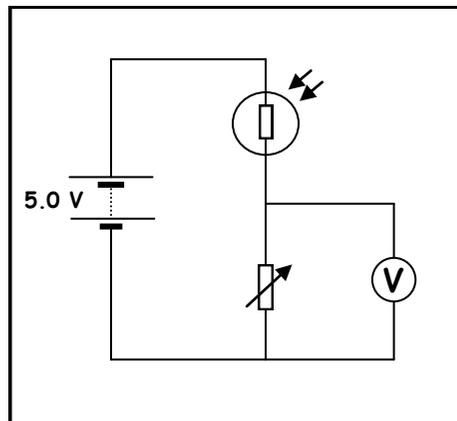
2. Calculate the **pd across the device** when it is connected between X and Y.

3. **Why** does the device fail to operate ?

(OCR AS Physics - Module 2822 - January 2001)

2 The diagram shows a potential divider circuit. The voltmeter has a very large resistance and the battery may be assumed to have negligible internal resistance.

For a particular intensity of light, the resistance of the LDR is **2.4 k $\Omega$** . The variable resistor is set on its maximum resistance of **4.7 k $\Omega$** .



(a) Calculate the **reading on the voltmeter.**

(b) State how the answer to (a) changes when the light intensity is **decreased**.

(OCR AS Physics part question - Module 2822 - May 2002)

3 The diagram shows a potential divider circuit designed as a touch sensor. The battery has **negligible** internal resistance and the voltmeter has **infinite** resistance.

(a) Explain why the voltmeter reading is **zero** when there is nothing connected between contacts X and Y.

(b) When the finger makes contact between X and Y, the voltmeter reading changes from **0 V** to **3.4 V** because of the electrical resistance of the skin. Use this information to calculate the **electrical resistance of the skin** between the two contacts.

(OCR AS Physics - Module 2822 - June 2005)

